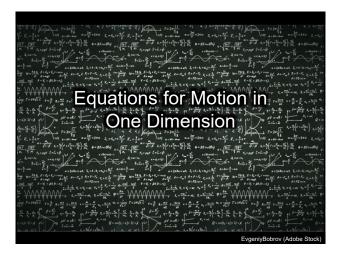
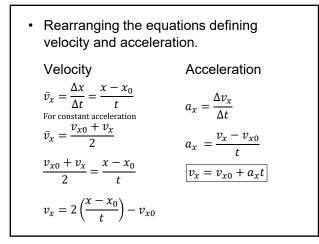
One Dimensional Motion



- The motion of an object can be described mathematically by using equations showing the displacement, velocity, and acceleration of an object at a given time.
 - · Notation and assumptions:
 - $t_0 = 0$, so t will represent the final time.
 - Motion will be in one dimension, using *x* for convenience.
 - Position and velocity will be represented as follows:
 - x_0, x initial and final position
 - v_0, v initial and final velocity
 - Acceleration is constant
 - $\bar{a} = a = \text{constant}$





• Set the two equations equal to each other and solve for *x*.

$$2\left(\frac{x-x_{0}}{t}\right) - v_{x0} = v_{x0} + a_{x}t$$
$$2\left(\frac{x-x_{0}}{t}\right) = 2v_{x0} + a_{x}t$$
$$x - x_{0} = v_{x0}t + \frac{1}{2}a_{x}t^{2}$$
$$x = x_{0} + v_{x0}t + \frac{1}{2}a_{x}t^{2}$$

• Solve the second equation for time and substitute it into the first equation.

$$v_{x} = v_{x0} + a_{x}t$$

$$t = \frac{v_{x} - v_{x0}}{a_{x}}$$

$$v_{x} = 2a_{x}\left(\frac{x - x_{0}}{v_{x} - v_{x0}}\right) - v_{x0}$$

• Rearrange the equation

$$v_{x} + v_{x0} = 2a_{x} \left(\frac{x - x_{0}}{v_{x} - v_{x0}} \right)$$

$$(v_{x} + v_{x0})(v_{x} - v_{x0}) = 2a_{x}(x - x_{0})$$

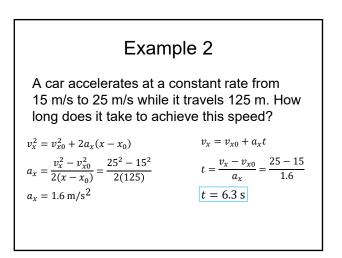
$$v_{x}^{2} - v_{x0}^{2} = 2a_{x}(x - x_{0})$$

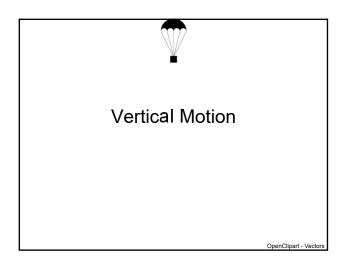
$$\boxed{v_{x}^{2} = v_{x0}^{2} + 2a_{x}(x - x_{0})}$$

Example 1

A rolling ball starts with a speed of 2.0 m/s and slows at a constant rate of 0.50 m/s². Calculate its velocity after 2.0 s.

 $v_x = v_{x0} + a_x t$ $v_x = 2 + (-0.5)2$ $v_x = 1 \text{ m/s}$



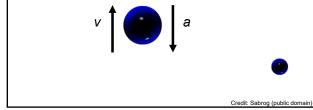


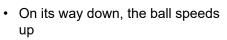


- When air resistance is not a factor, **all** objects near Earth's surface fall with an acceleration of about 9.8 m/s².
 - Although this value decreases slightly with increasing altitude, it may be assumed to be essentially constant.
- The value of 9.8 m/s² is labeled **g** and is referred to as the **acceleration due to gravity**.
- Since gravity pulls objects towards the earth's surface, this acceleration is **always** down (negative).

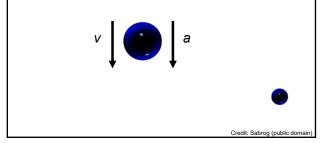
What happens when a ball is thrown straight up in the air?

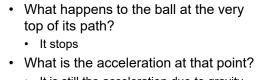
- On its way up, the ball slows down
 - The acceleration due to gravity is in the opposite direction of the velocity of the ball



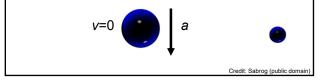


• The acceleration due to gravity is in the same direction as the velocity of the ball





- It is still the acceleration due to gravity and it is still down
- The **direction** of the ball is changing instead of the speed.





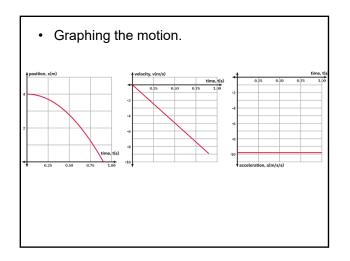




Example 1

A ball is dropped from a height of 4.0 m. What is its velocity just before it hits the ground?

 $v_x^2 = v_{x0}^2 + 2a_x(x - x_0)$ $v_x = \sqrt{2a_x x} = \sqrt{2(-9.8)(-4.0)}$ $v_x = 8.9 \text{ m/s}$





Example 2

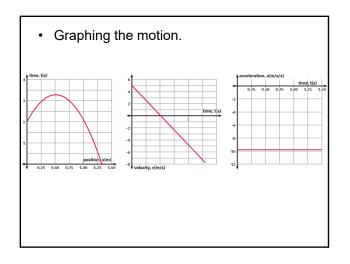
A ball is thrown straight up in the air with a velocity of 5.0 m/s from a height of 2.0 m.

- a) How high above the ground does the ball go?
- b) How long is the ball in the air?

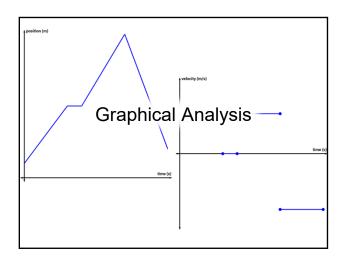
a) How high above the ground does the ball go?

$$v_x^2 = v_{x0}^2 + 2a_x(x - x_0)$$

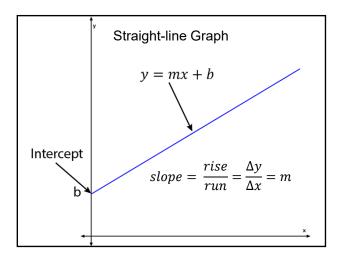
 $x = \frac{-v_{x0}^2}{2a_x} + x_0 = \frac{-(5^2)}{2(-9.8)} + 2$
 $x = 3.3 \text{ m}$
b) How long is the ball in the air?
 $x = x_0 + v_{x0}t + \frac{1}{2}a_xt^2$
 $0 = 2 + 5t + \frac{1}{2}(-9.8)t^2$
 $4.9t^2 - 5t - 2 = 0$
 $t = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(4.9)(-2)}}{2(4.9)} = 1.3, \xrightarrow{\sim} 1$
 $t = 1.3 \text{ s}$



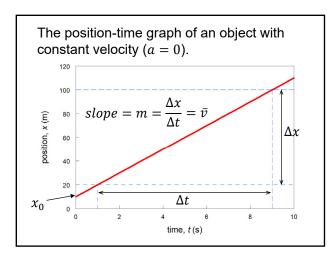










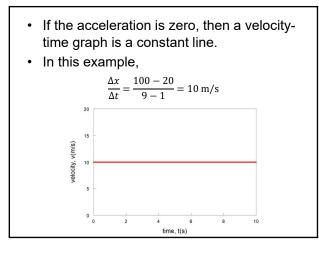


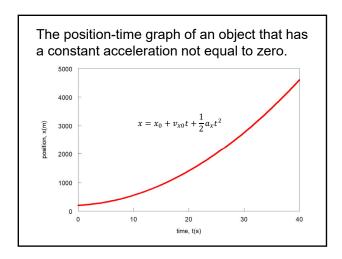


- Substituting into the equation of a line gives y = mx + b $x = \bar{v}t + x_0$
- Since velocity is constant $\bar{v} = v_{x0}$

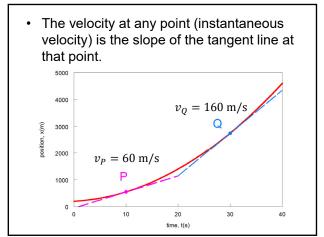
$$x = x_0 + v_{x0}t$$

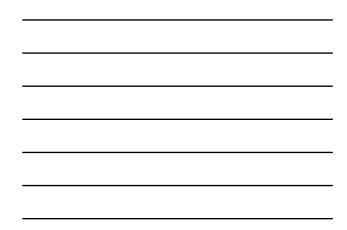
Note: This is the equation that we derived earlier with a = 0.

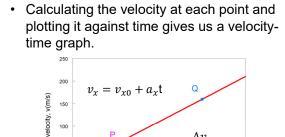


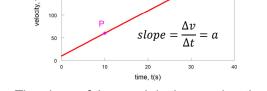












• The slope of the graph is the acceleration.

